JEE 2015 Physics

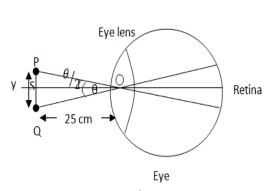


SelfStudy.in

26. Assuming human pupil to have a radius of 0.25 cm and a comfortable viewing distance of 25 cm, the minimum separation between two objects that human eye can resolve at 500 nm wavelength is :

- (1) 1 µm
- (2) 30 µm
- (3) 100 μm
- (4) 300 μm

Answer:



Minimum distance of separation P and Q of two points which can be distinctly seen by eye lens is resolving power. Let PQ makes an angle θ .

D= diameter of aperture= $0.25 \times 2 \times 10^{-2} m$ Then we know that

$$\theta = 1.22 \frac{\lambda}{D} = 1.22 \frac{500 \times 10^{-9}}{0.25 \times 2 \times 10^{-2}} \rightarrow (1)$$

In
$$\triangle POS : tan \frac{\theta}{2} = \frac{y/2}{0.25} = \frac{y}{2 \times 0.25}$$

$$\theta$$
 being small, $\tan \frac{\theta}{2} \approx \frac{\theta}{2} = \frac{y}{2 \times 0.25}$ or $\theta = \frac{y}{0.25}$

putting value from (1):

$$\frac{1.22 \times 500 \times 10^{-9}}{0.25 \times 2 \times 10^{-2}} = \frac{y}{0.25}$$

or
$$y = 305 \times 10^{-7} m \approx 30 \mu m$$

Correct option is (2) $30\mu m$.